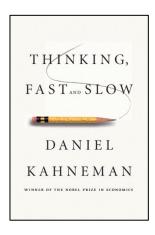
Bayesian reasoning in the social domain

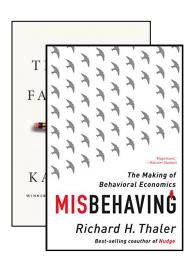
Jack Cao April 24, 2019



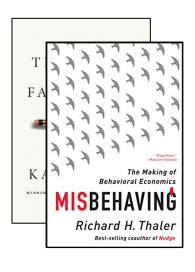






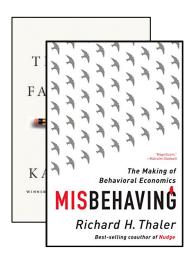










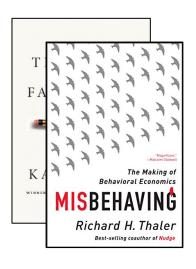
















"The theory that would not die..." Sharon McGrayne, Science Writer

"...arguably the most powerful mechanism created for processing data and knowledge."

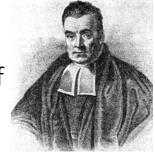
Jim Berger, Statistician

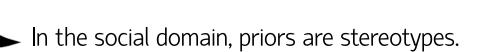


In the social domain, priors are stereotypes.

Locksley et al. (1980) Krosnick et al. (1990) Jussim (2012)





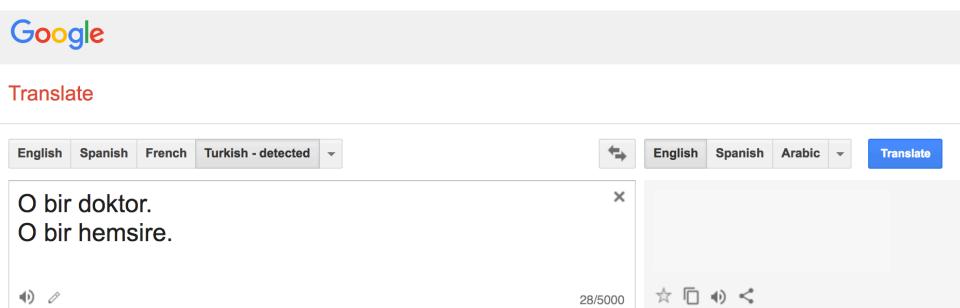


Locksley et al. (1980) Krosnick et al. (1990) Jussim (2012)

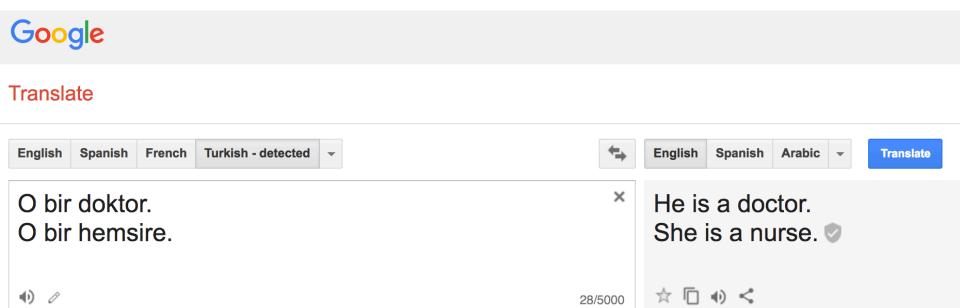


The law privileges Egalitarian values over Bayesian principles.

Artificial Intelligence that's more Bayesian than egalitarian



Artificial Intelligence that's more Bayesian than egalitarian



 People undermine their commitment to egalitarian values by making Bayesian judgments

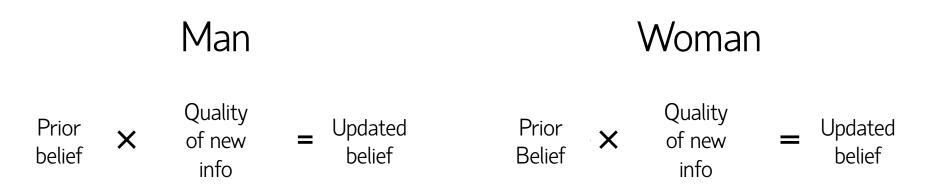
People undermine their commitment to egalitarian values by making Bayesian judgments

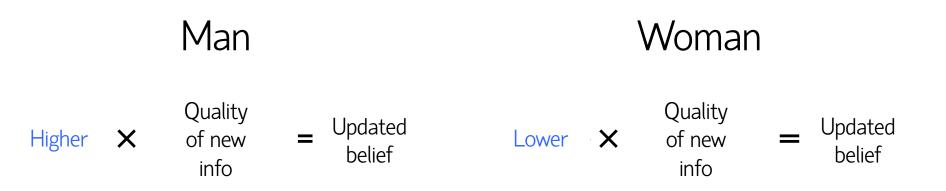
2. Formalizing "egalitarian values"

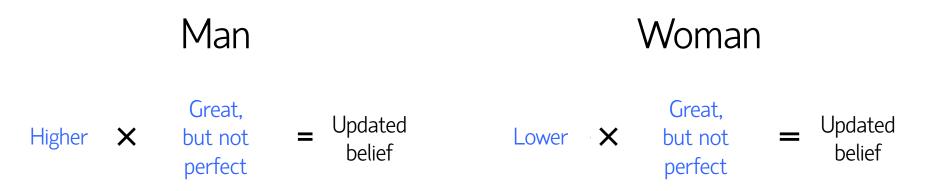
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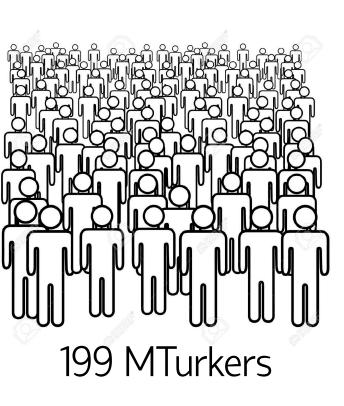




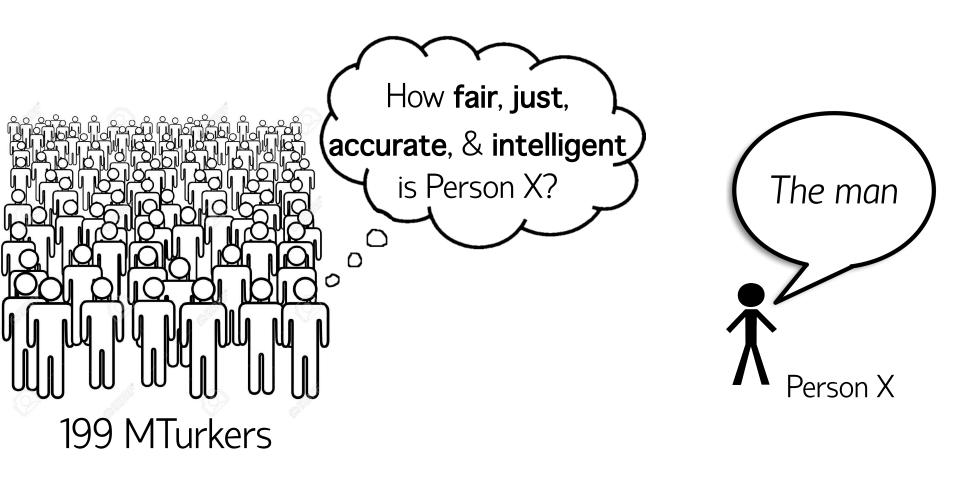


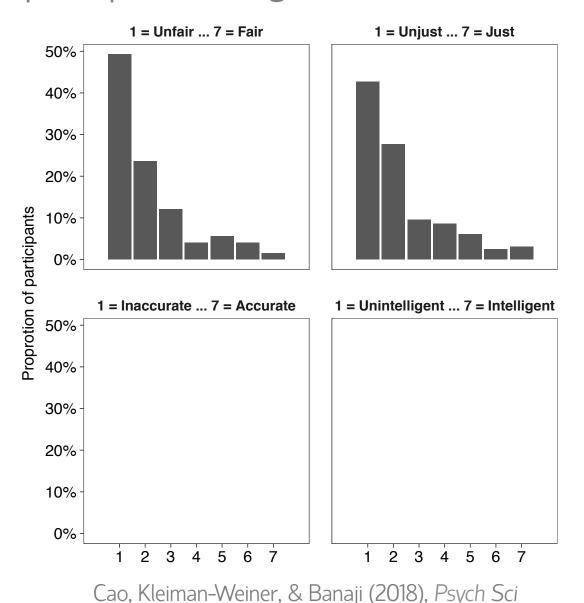


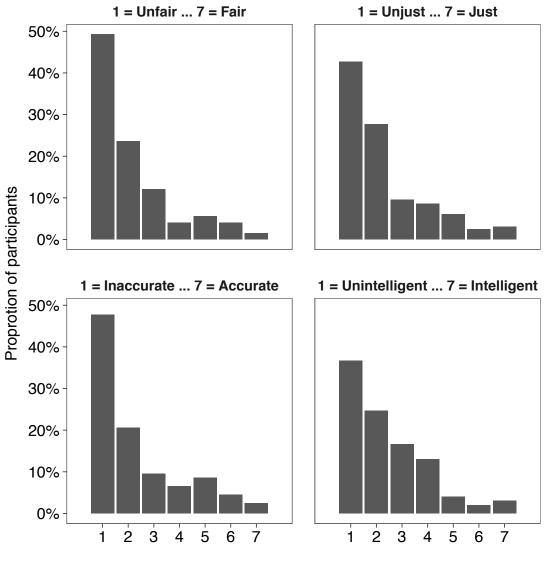




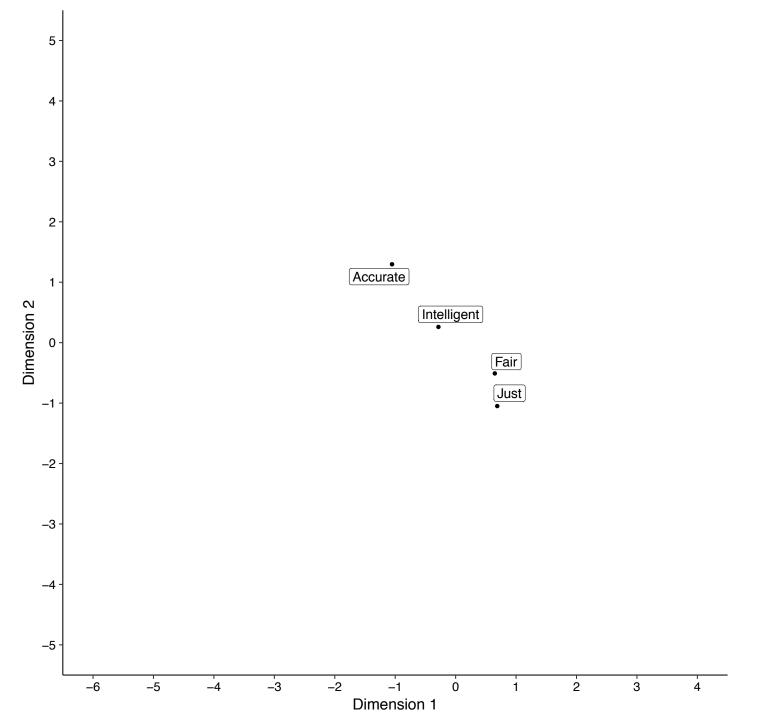


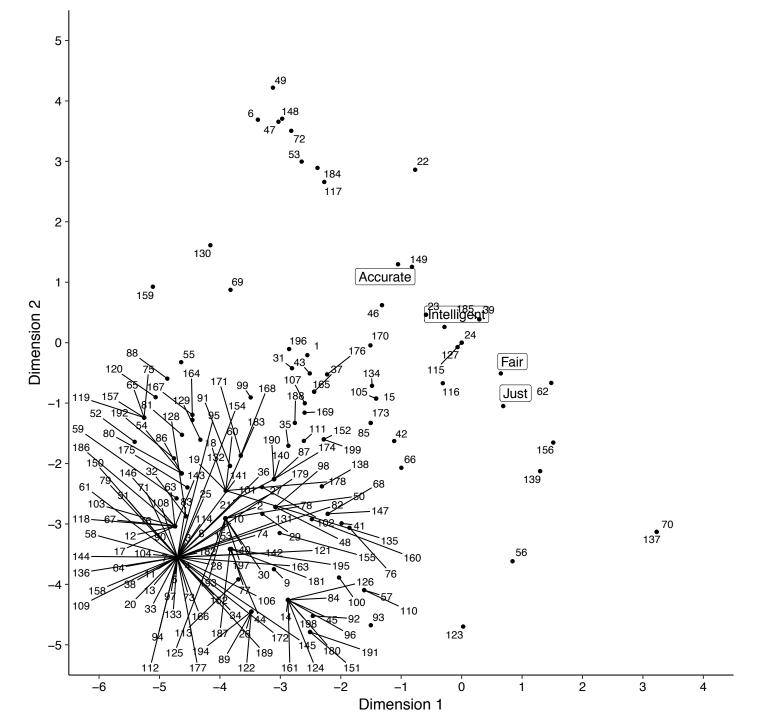


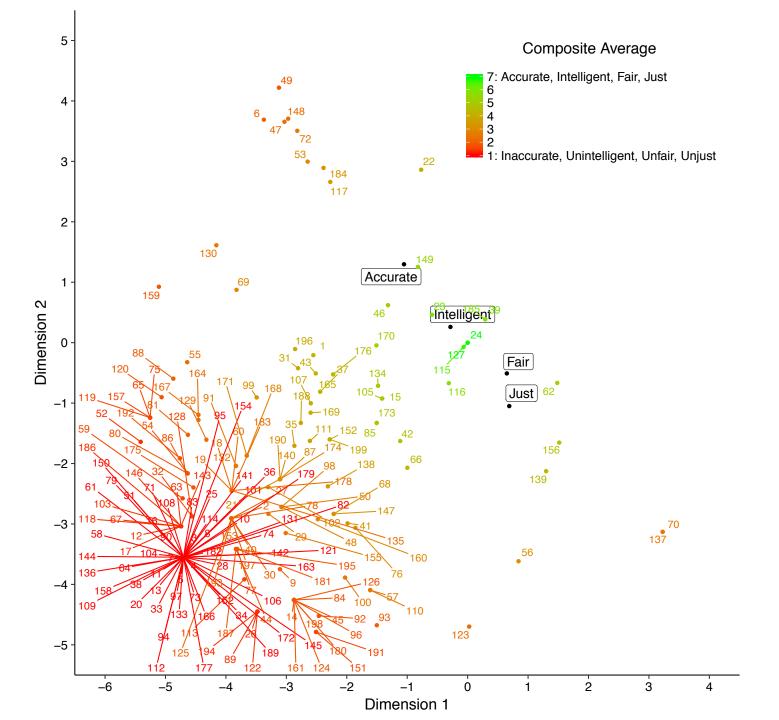


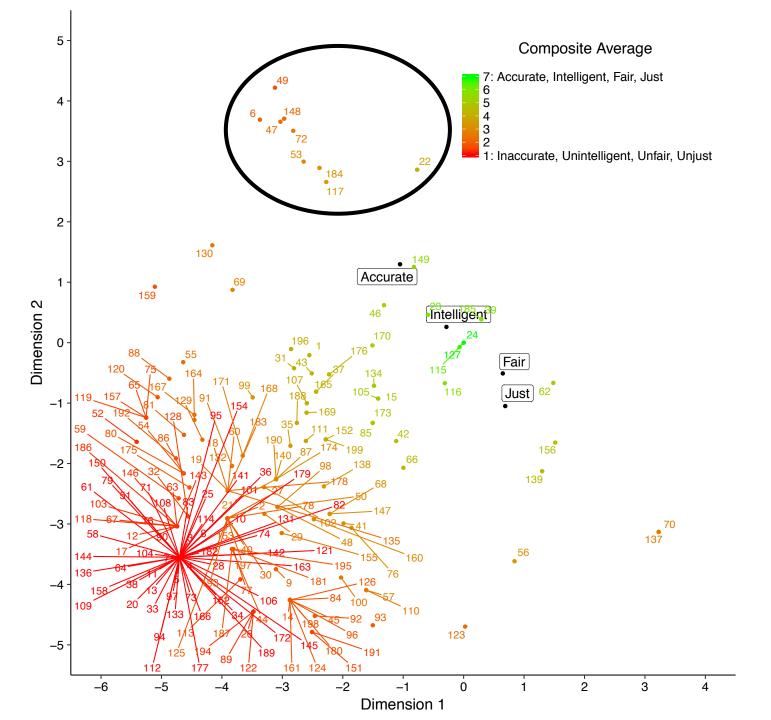


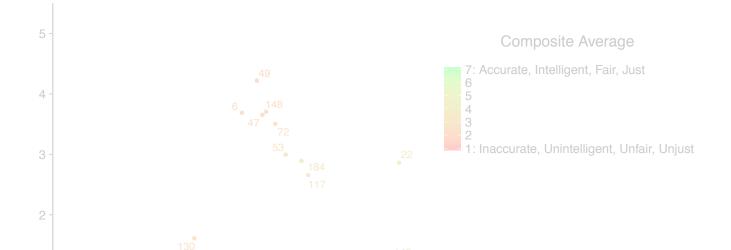
Cao, Kleiman-Weiner, & Banaji (2018), Psych Sci



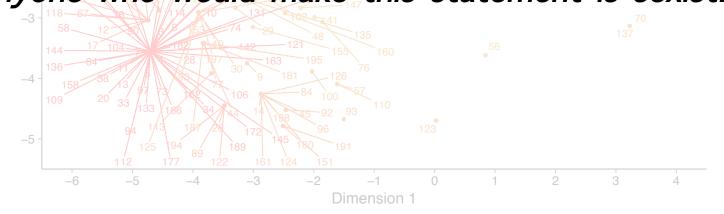


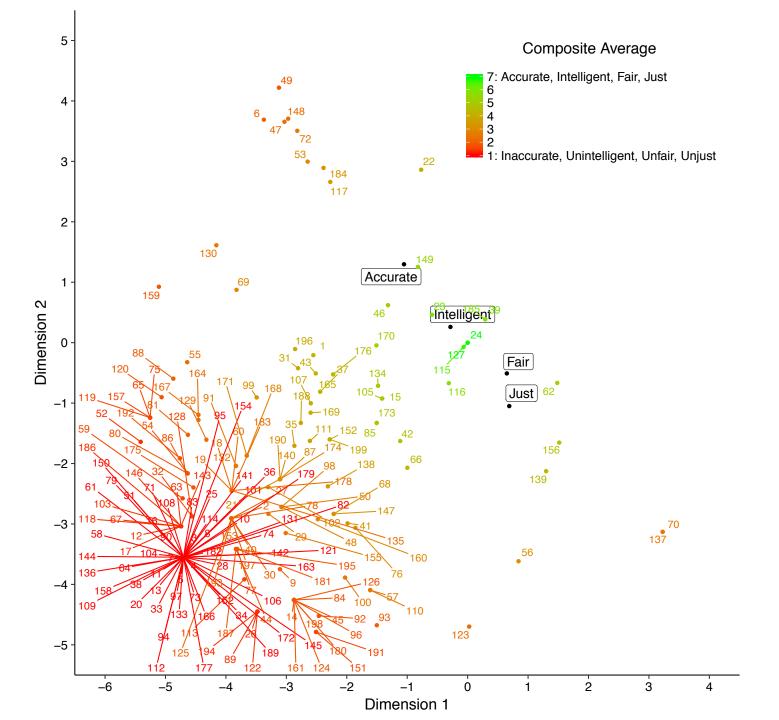


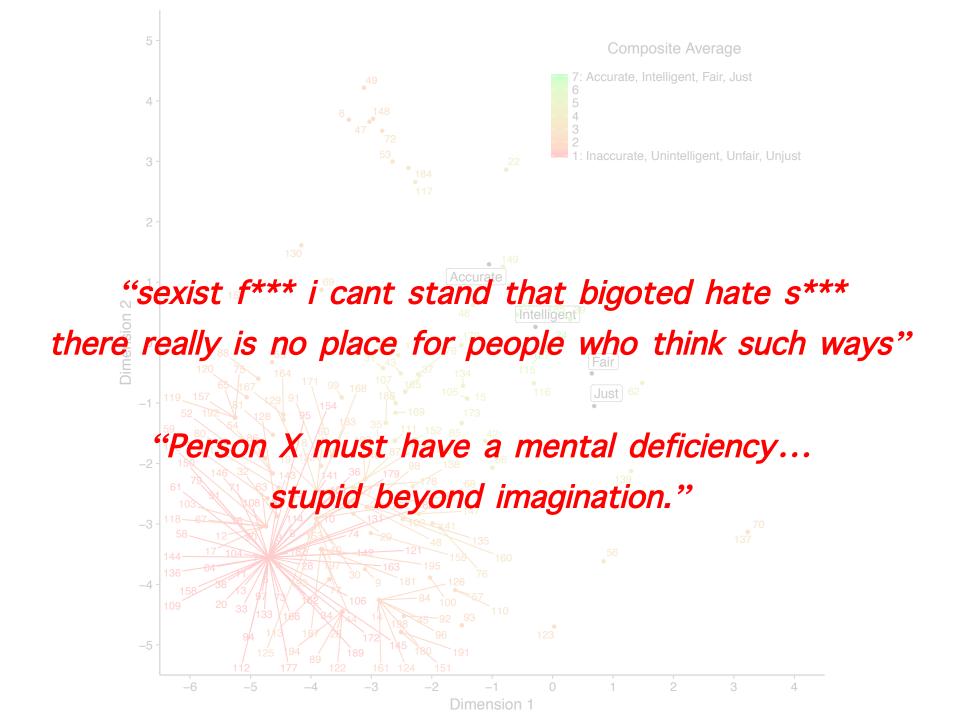


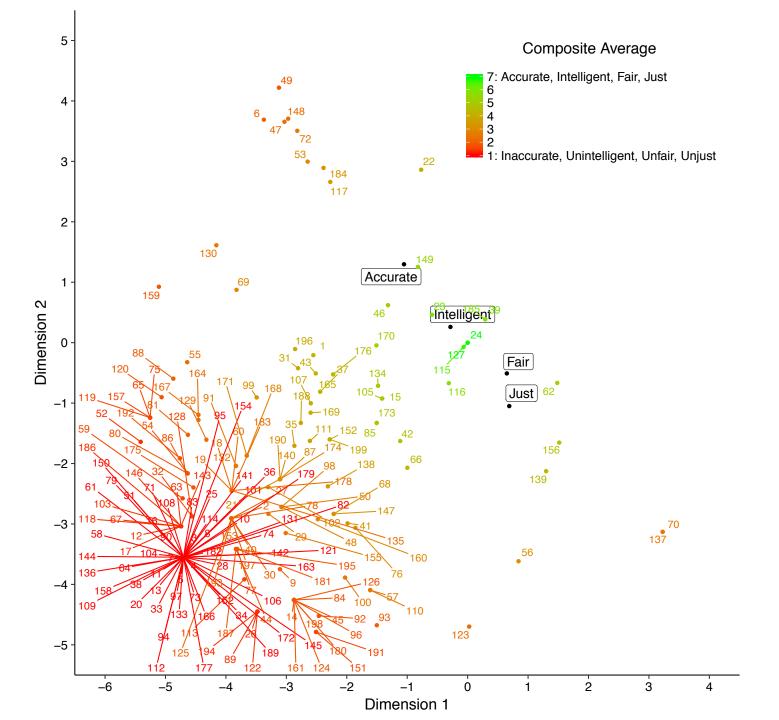


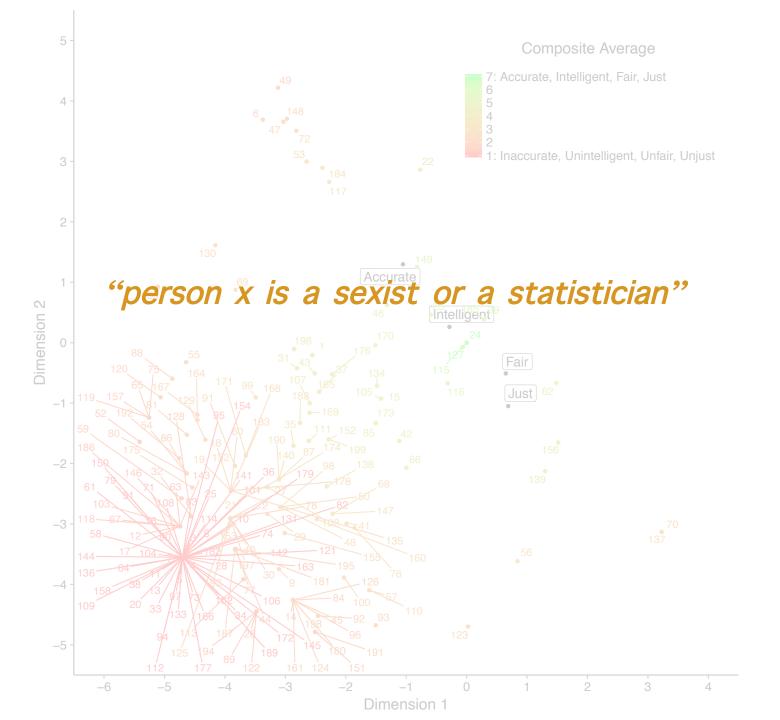
"I agree with Person X because statistics indicate that there are less women surgeon [sic] compared to men. However, this does not mean I like it. It is sad that women are under-represented than man [sic] in surgery, and i believe that anyone who would make this statement is sexist."

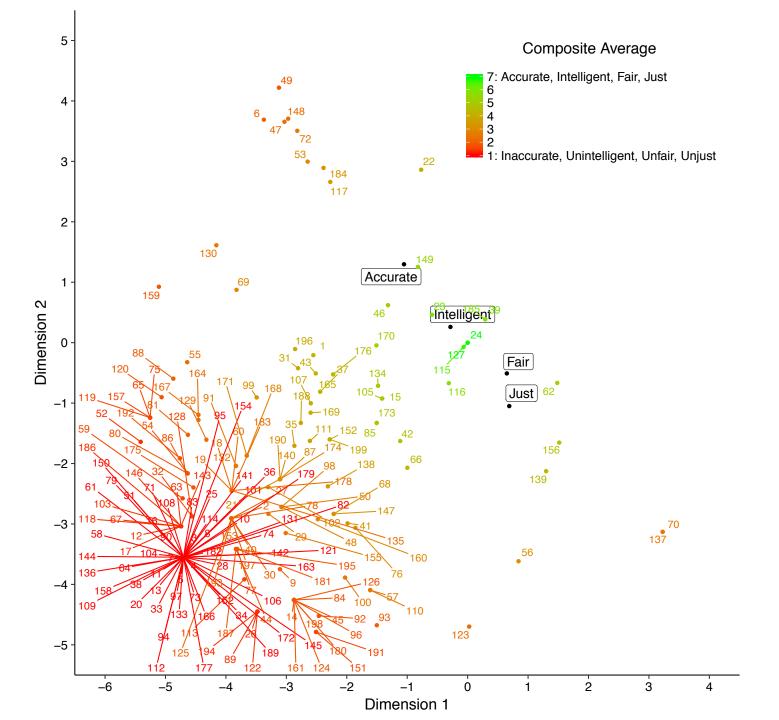






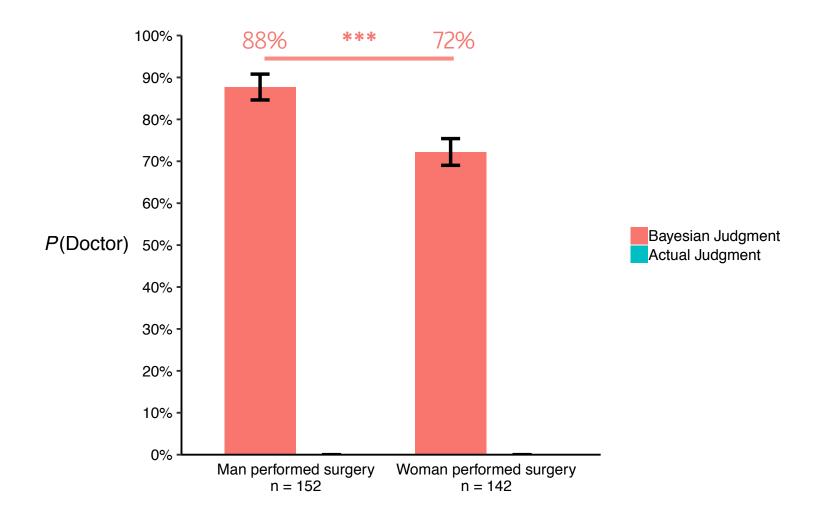




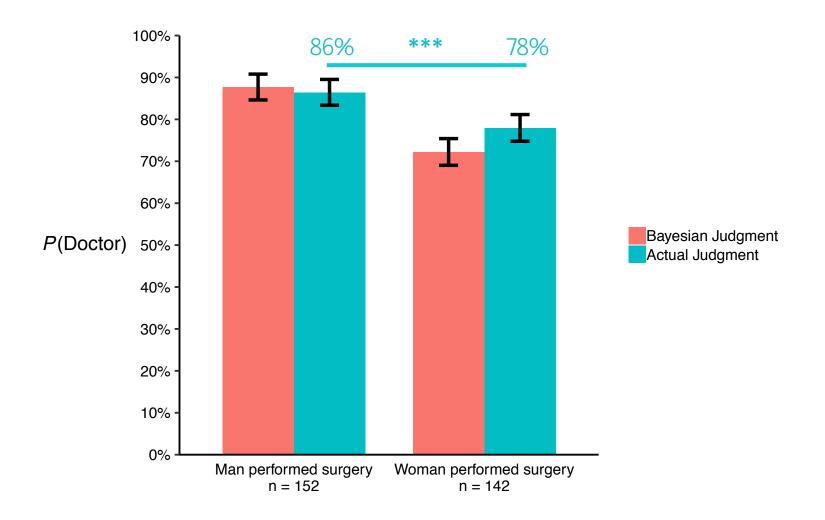




How likely is a man vs. a woman to be a doctor given that each performed surgery?



Cao, Kleiman-Weiner, & Banaji (2018), Psych Sci



Cao, Kleiman-Weiner, & Banaji (2018), Psych Sci

People undermine their commitment to egalitarian values by making Bayesian judgments

2. Formalizing "egalitarian values"

3. Google Images as a proxy for the social environment

1. People undermine their commitment to egalitarian values by making Bayesian judgments

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How do you go from something like this...



to something like this...



When outcomes depend on social group, ceteris paribus

When outcomes depend on social group, ceteris paribus

Policing Correll et al. (2007), JPSP

Medicine Hoffman, Trawalter, et al. (2016), PNAS

Hiring Moss-Racusin et al. (2012), PNAS

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P(Shoot | Unarmed, White) < P(Shoot | Unarmed, Black)

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P(Shoot | Unarmed, White) < P(Shoot | Unarmed, Black)

 $P(Undertreat \mid In Pain, White) < P(Undertreat \mid In Pain, Black)$

<u>Unequal false positive rates, FPRs</u> P(Shoot | Unarmed, White) < P(Shoot | Unarmed, Black)

 $P(Undertreat \mid In Pain, White) < P(Undertreat \mid In Pain, Black)$

<u>Unequal false positive rates, FPRs</u> P(Shoot | Unarmed, White) < P(Shoot | Unarmed, Black)

<u>Unequal false negative rates, FNRs</u> P(Undertreat | In Pain, White) < P(Undertreat | In Pain, Black)

<u>Unequal false positive rates, FPRs</u> P(Shoot | Unarmed, White) < P(Shoot | Unarmed, Black)

Unequal false negative rates, FNRs

P(Undertreat | In Pain, White) < P(Undertreat | In Pain, Black)

<u>Unequal positive predictive values, PPVs</u>

Not egalitarian

<u>Unequal false positive rates, FPRs</u> P(Shoot | Unarmed, White) < P(Shoot | Unarmed, Black)

<u>Unequal false negative rates, FNRs</u> P(Undertreat | In Pain, White) < P(Undertreat | In Pain, Black)

<u>Unequal positive predictive values, PPVs</u> P(Hire | Qualified, Female) < P(Hire | Qualified, Male)

Egalitarian

Equal false positive rates, FPRs

P(Shoot | Unarmed, White) = P(Shoot | Unarmed, Black)

Equal false negative rates, FNRs

 $P(Undertreat \mid In Pain, White) = P(Undertreat \mid In Pain, Black)$

Equal positive predictive values, PPVs

 $P(Hire \mid Qualified, Female) = P(Hire \mid Qualified, Male)$

Why these three ways of thinking about egalitarian values?

$$FNR_{Group A} = FNR_{Group B}$$

Why these three ways of thinking about egalitarian values?

$$FNR_{Group A} = FNR_{Group B}$$

When base rates between Group A and Group B differ, all three definitions cannot be simultaneously met. At least one must be given up. Kleinberg, Mullainathan, & Raghavan (2016)

$$P(\text{cancer} \mid \text{pos}) = \frac{P(\text{pos} \mid \text{cancer}) \times P(\text{cancer})}{P(\text{pos} \mid \text{cancer}) \times P(\text{cancer}) + P(\text{pos} \mid \text{no cancer}) \times P(\text{no cancer})}$$

$$P(\text{pos} | \text{cancer}) \times P(\text{cancer})$$

$$P(\text{pos} | \text{cancer}) \times P(\text{pos} | \text{no cancer}) \times P(\text{no cancer})$$

$$\Gamma(\text{pos} | \text{cancer}) \times P(\text{pos} | \text{cancer}) \times P(\text{no cancer})$$

$$P(\text{cancer} \mid \text{pos}) = \frac{[1 - P(\text{neg} \mid \text{cancer})] \times P(\text{cancer})}{[1 - P(\text{neg} \mid \text{cancer})] \times P(\text{cancer}) + P(\text{pos} \mid \text{no cancer}) \times [1 - P(\text{cancer})]}$$

$$P(\text{pos} | \text{cancer}) \times P(\text{cancer})$$

$$= \frac{P(\text{pos} | \text{cancer}) \times P(\text{cancer})}{P(\text{pos} | \text{cancer}) \times P(\text{pos} | \text{no cancer}) \times P(\text{no cancer})}$$

$$P(\text{cancer} \mid \text{pos}) = \frac{[1 - P(\text{neg} \mid \text{cancer})] \times P(\text{cancer})}{[1 - P(\text{neg} \mid \text{cancer})] \times P(\text{cancer}) + P(\text{pos} \mid \text{no cancer}) \times [1 - P(\text{cancer})]}$$

$$PPV = \frac{[1-FNR] \times BR}{[1-FNR] \times BR + FPR \times [1-BR]}$$

$$P(\text{cancer} | \text{pos}) = \frac{P(\text{pos} | \text{cancer}) \times P(\text{cancer})}{P(\text{pos} | \text{cancer}) \times P(\text{cancer}) + P(\text{pos} | \text{no cancer}) \times P(\text{no cancer})}$$

$$P(\text{cancer} \mid \text{pos}) = \frac{[1 - P(\text{neg} \mid \text{cancer})] \times P(\text{cancer})}{[1 - P(\text{neg} \mid \text{cancer})] \times P(\text{cancer}) + P(\text{pos} \mid \text{no cancer}) \times [1 - P(\text{cancer})]}$$

$$PPV = \frac{[1-FNR] \times BR}{[1-FNR] \times BR + FPR \times [1-BR]}$$

$$FPR = \frac{BR}{[1-BR]} \times \frac{[1-PPV]}{PPV} \times [1-FNR]$$

$$FPR_w = \frac{BR_w}{1 - BR_w} \times \frac{1 - PPV_w}{PPV_w} \times [1 - FNR_w]$$

$$FPR_m = \frac{BR_m}{1 - BR_m} \times \frac{1 - PPV_m}{PPV_m} \times [1 - FNR_m]$$

$$FPR_{w} = \frac{BR_{w}}{1 - BR_{w}} \times \frac{1 - PPV_{w}}{PPV_{w}} \times [1 - FNR_{w}]$$

$$FPR_{m} = \frac{BR_{m}}{1 - BR_{m}} \times \frac{1 - PPV_{m}}{PPV_{m}} \times [1 - FNR_{m}]$$

Meet two definitions of fairness

$$PPV_w = PPV_m$$

$$FNR_w = FNR_m$$

$$\frac{FPR_{w}}{FPR_{m}} = \frac{\frac{BR_{w}}{1 - BR_{w}} \times \frac{1 - PPV_{w}}{PPV_{w}} \times [1 - FNR_{w}]}{\frac{BR_{m}}{1 - BR_{m}} \times \frac{1 - PPV_{m}}{PPV_{m}} \times [1 - FNR_{m}]}$$

$$FPR_{w} = \frac{BR_{w}}{1 - BR_{w}} \times \frac{1 - PPV_{w}}{PPV_{w}} \times [1 - FNR_{w}]$$

$$FPR_{m} = \frac{BR_{m}}{1 - BR_{m}} \times \frac{1 - PPV_{m}}{PPV_{m}} \times [1 - FNR_{m}]$$

Meet two definitions of fairness
$$PPV_w = PPV_m$$

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$$\frac{\text{FPR}_{w}}{\text{FPR}_{m}} = \frac{\frac{\text{BR}_{w}}{1 - \text{BR}_{w}} \times \frac{1 - \text{PPV}_{w}}{\text{PPV}_{w}} \times [1 - \text{FNR}_{w}]}{\frac{\text{BR}_{m}}{1 - \text{BR}_{m}} \times \frac{1 - \text{PPV}_{m}}{\text{PPV}_{m}} \times [1 - \text{FNR}_{m}]}$$

$$FPR_{w} = \frac{BR_{w}}{1 - BR_{w}} \times \frac{1 - PPV_{w}}{PPV_{w}} \times [1 - FNR_{w}]$$

$$FPR_{m} = \frac{BR_{m}}{1 - BR_{m}} \times \frac{1 - PPV_{m}}{PPV_{m}} \times [1 - FNR_{m}]$$

Meet two definitions of fairness

$$PPV_w = PPV_m$$

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$$\frac{\text{FPR}_{w}}{\text{FPR}_{m}} = \frac{\frac{BR_{w}}{1 - BR_{w}} \times \frac{1 - PPV_{w}}{PPV_{w}} \times [1 - PNR_{w}]}{\frac{BR_{m}}{1 - BR_{m}} \times \frac{1 - PPV_{m}}{PPV_{m}} \times [1 - ENR_{m}]}$$

$$\frac{FPR_w}{FPR_m} = \frac{\frac{BR_w}{1 - BR_w}}{\frac{BR_m}{1 - BR_m}}$$

$$FPR_{w} = \frac{BR_{w}}{1 - BR_{w}} \times \frac{1 - PPV_{w}}{PPV_{w}} \times [1 - FNR_{w}]$$

$$FPR_{m} = \frac{BR_{m}}{1 - BR_{m}} \times \frac{1 - PPV_{m}}{PPV_{m}} \times [1 - FNR_{m}]$$

Meet two definitions of fairness

$$PPV_w = PPV_m$$

$$FNR_w = FNR_m$$

$$\frac{FPR_{w}}{FPR_{m}} = \frac{\frac{BR_{w}}{1 - BR_{w}} \times \frac{1 - PPV_{w}}{PPV_{w}} \times [1 - FNR_{w}]}{\frac{BR_{m}}{1 - BR_{m}} \times \frac{1 - PPV_{m}}{PPV_{m}} \times [1 - FNR_{m}]}$$

$$\frac{FPR_w}{FPR_m} = \frac{\frac{BR_w}{1 - BR_w}}{\frac{BR_m}{1 - BR_m}}$$

$$FPR_w = \frac{BR_w}{BR_m} \times \frac{[1 - BR_m]}{[1 - BR_w]} \times FPR_m$$

$$FPR_{w} = \frac{BR_{w}}{1 - BR_{w}} \times \frac{1 - PPV_{w}}{PPV_{w}} \times [1 - FNR_{w}]$$

$$FPR_{m} = \frac{BR_{m}}{1 - BR_{m}} \times \frac{1 - PPV_{m}}{PPV_{m}} \times [1 - FNR_{m}]$$

Meet two definitions of fairness $PPV_w = PPV_m$

$$FNR_w = FNR_m$$

$$\frac{FPR_{w}}{FPR_{m}} = \frac{\frac{BR_{w}}{1 - BR_{w}} \times \frac{1 - PPV_{w}}{PPV_{w}} \times [1 - FNR_{w}]}{\frac{BR_{m}}{1 - BR_{m}} \times \frac{1 - PPV_{m}}{PPV_{m}} \times [1 - FNR_{m}]}$$

Cannot meet third definition of fairness $FPR_w = FPR_m$

Breast cancer is more common among women than men

$$\frac{FPR_w}{FPR_m} = \frac{\frac{BR_w}{1 - BR_w}}{\frac{BR_m}{1 - BR_m}}$$

$$FPR_w = \frac{BR_w}{BR_m} \times \frac{[1 - BR_m]}{[1 - BR_w]} \times FPR_m$$

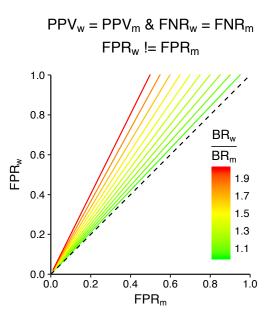
$$FPR_{w} = \frac{BR_{w}}{1 - BR_{w}} \times \frac{1 - PPV_{w}}{PPV_{w}} \times [1 - FNR_{w}]$$

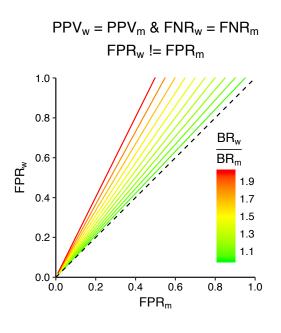
$$FPR_m = \frac{BR_m}{1 - BR_m} \times \frac{1 - PPV_m}{PPV_m} \times [1 - FNR_m]$$

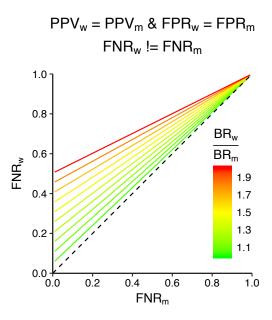
$$\frac{\text{FPR}_{w}}{\text{FPR}_{m}} = \frac{\frac{\text{BR}_{w}}{1 - \text{BR}_{w}} \times \frac{1 - \text{PPV}_{w}}{\text{PPV}_{w}} \times [1 - \text{FNR}_{w}]}{\frac{\text{BR}_{m}}{1 - \text{BR}_{m}} \times \frac{1 - \text{PPV}_{m}}{\text{PPV}_{m}} \times [1 - \text{FNR}_{m}]}$$

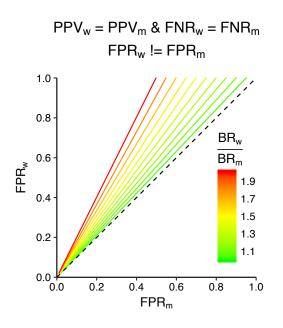
$$\frac{FPR_w}{FPR_m} = \frac{\frac{BR_w}{1 - BR_w}}{\frac{BR_m}{1 - BR_m}}$$

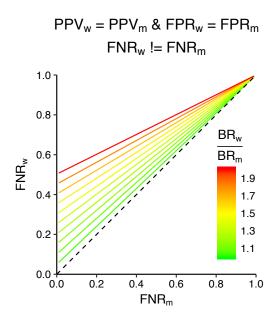
$$FPR_w = \frac{BR_w}{BR_m} \times \frac{[1 - BR_m]}{[1 - BR_w]} \times FPR_m$$

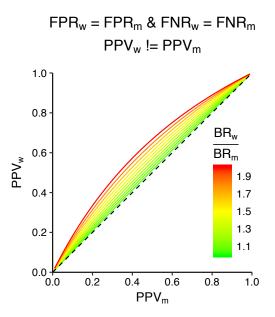


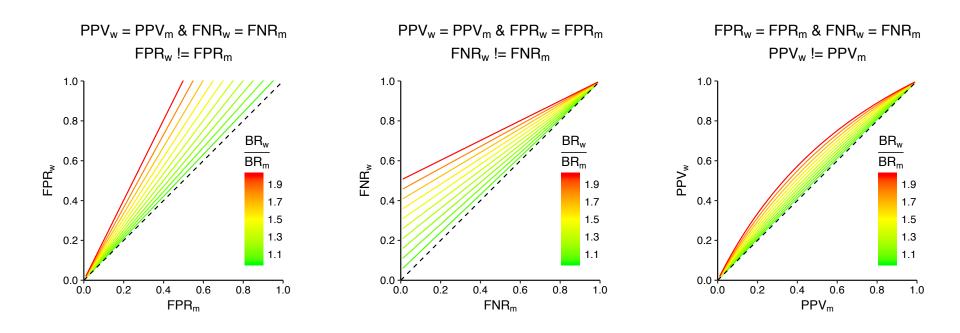












Of the three "worlds" depicted above, which is preferred? Which notion of fairness is valued more? Which is valued less?





Bail eligibility for defendants
Bank loans
Whether a post is fake news

Machine Bias

There's software used across the country to predict future criminals. And it's biased against blacks.

by Julia Angwin, Jeff Larson, Surya Mattu and Lauren Kirchner, ProPublica
May 23, 2016

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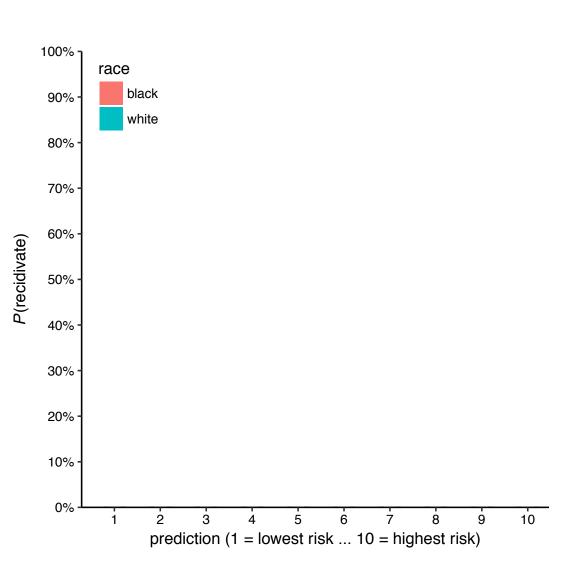
Machine Bias

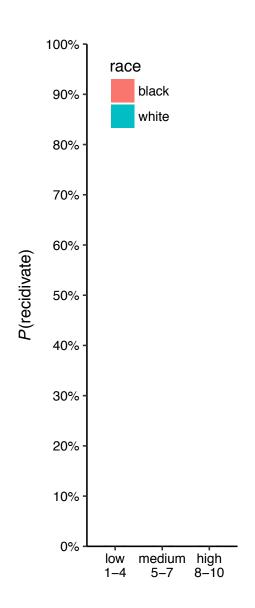
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False Positives, False Negatives, and False Analyses: A Rejoinder to "Machine Bias: There's Software Used Across the Country to Predict Future Criminals. And It's Biased Against Blacks."

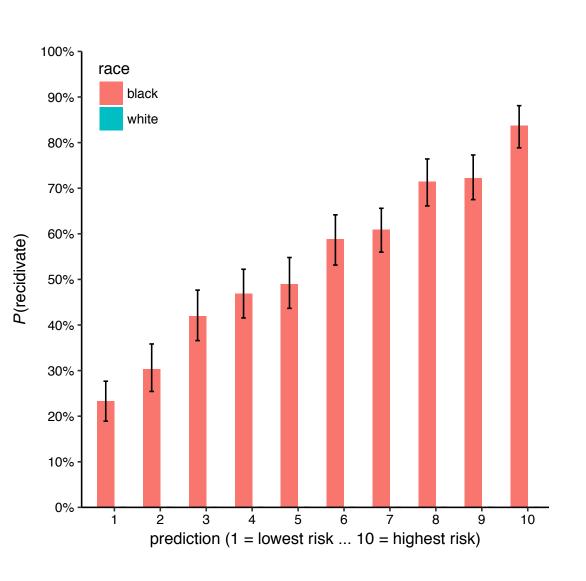
Anthony W. Flores
California State University, Bakersfield
Kristin Bechtel
Crime and Justice Institute at CRJ
Christopher T. Lowenkamp
Administrative Office of the United States Courts
Probation and Pretrial Services Office

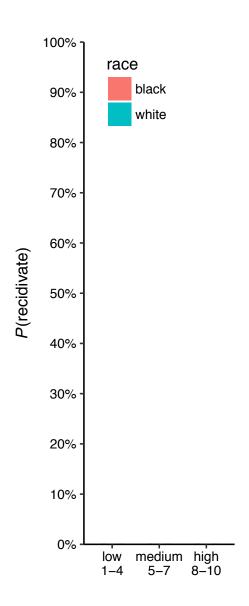
 $PPV_{black} = PPV_{white}$ P(recidivate | risk score, black) = P(recidivate | risk score, white)



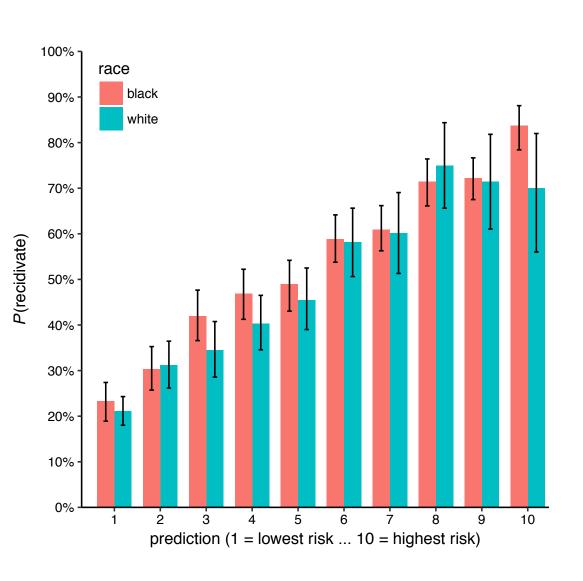


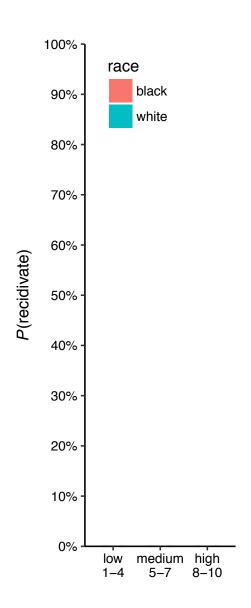
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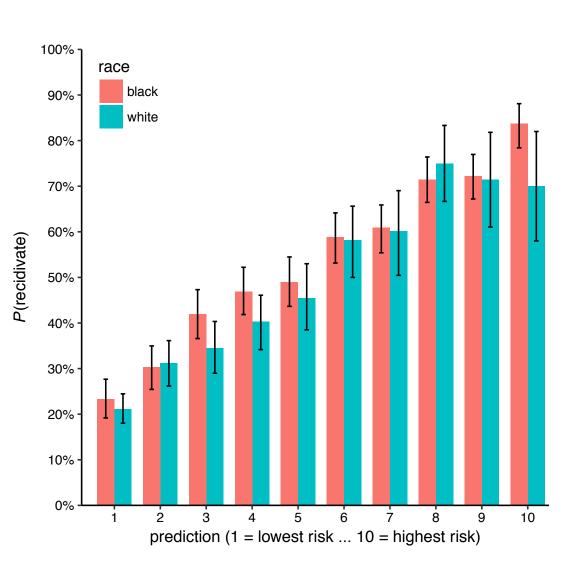


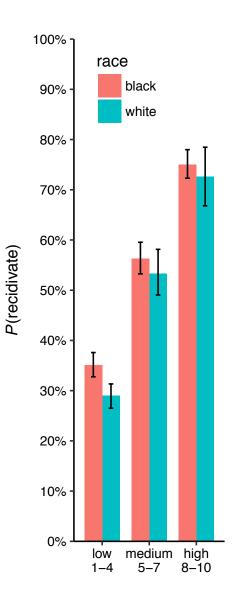
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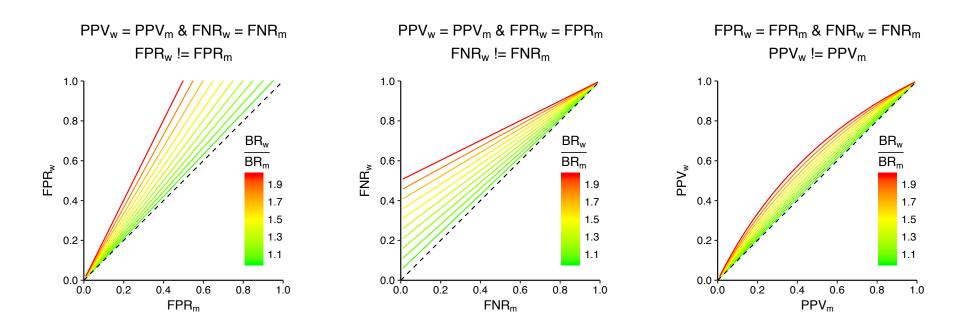


 $PPV_{black} = PPV_{white}$ P(recidivate | risk score, black) = P(recidivate | risk score, white)





The sinister tradeoff



Of the three "worlds" depicted above, which is preferred? Which notion of fairness is valued more? Which is valued less?

What judgments do people make when Bayesian principles and egalitarian values are at stake?

1. People undermine their commitment to egalitarian values by making Bayesian judgments

2. Formalizing "egalitarian values"

3. Google Images as a proxy for the social environment

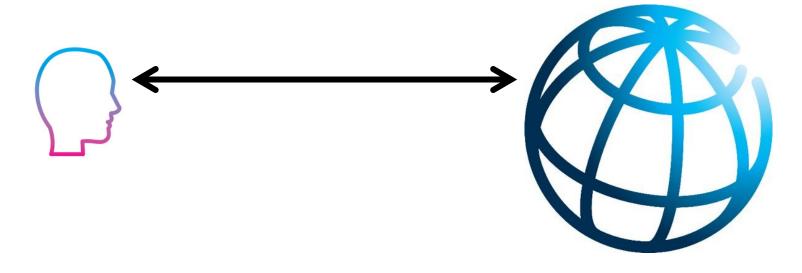
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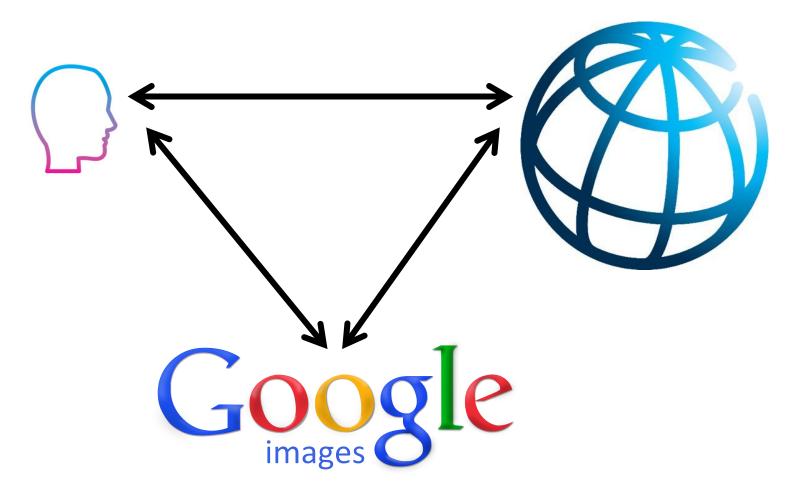
2. Formalizing "egalitarian values"

3. Google Images as a proxy for the social environment

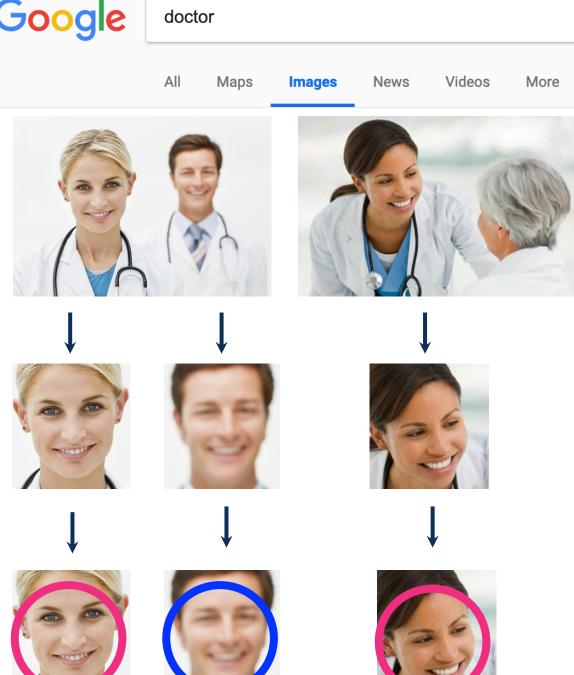
- 1. Pictures of people matter a great deal
- 2. There's some relationship between the content in our minds and the content in the world



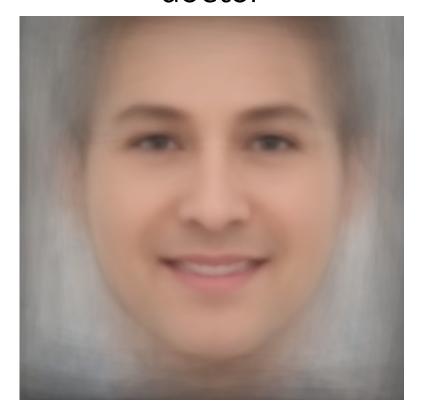
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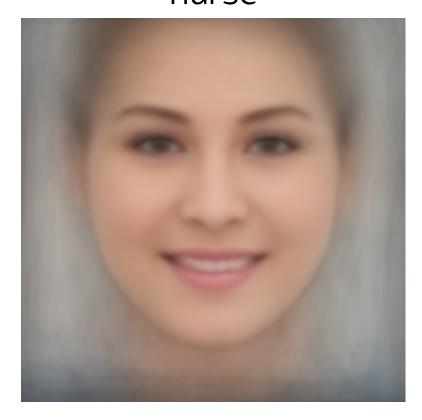




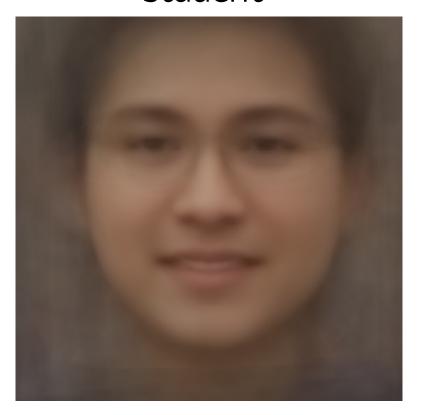
"doctor"



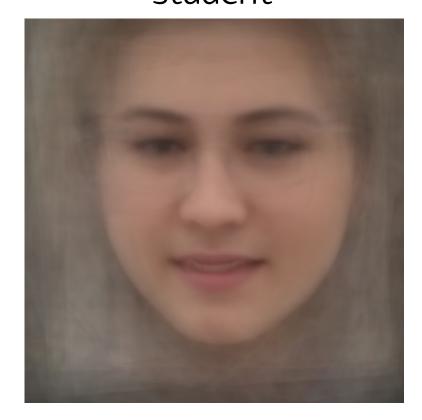
"nurse"



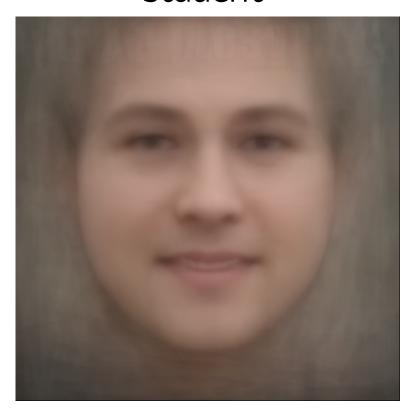
"computer science student"



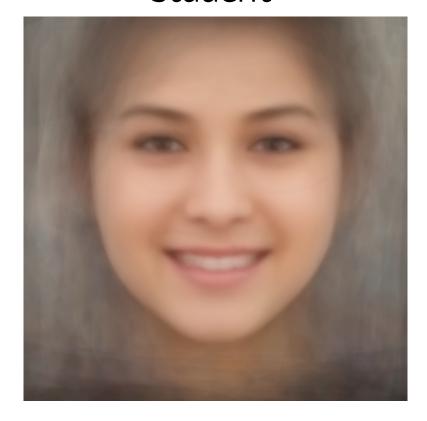
"biology student"



"philosophy student"



"education student"



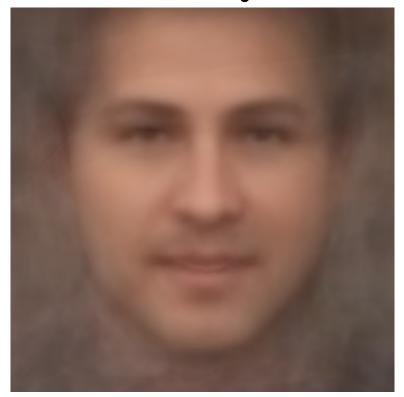
"intelligent person"



"sensitive person"



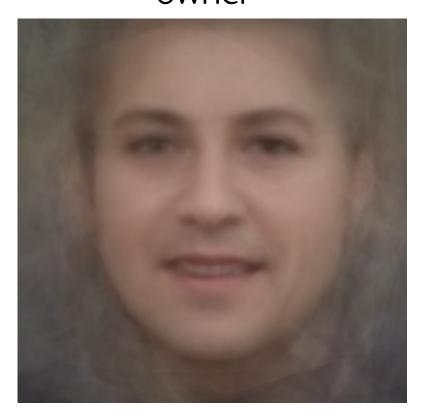
"person drinking whiskey"



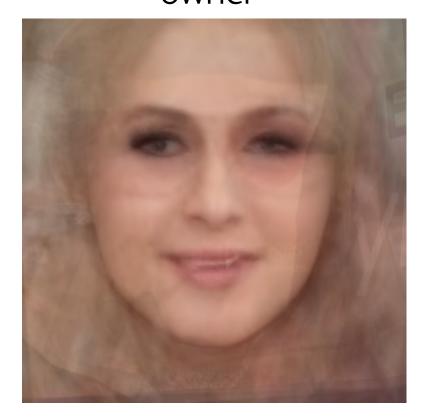
"person drinking cosmopolitan"



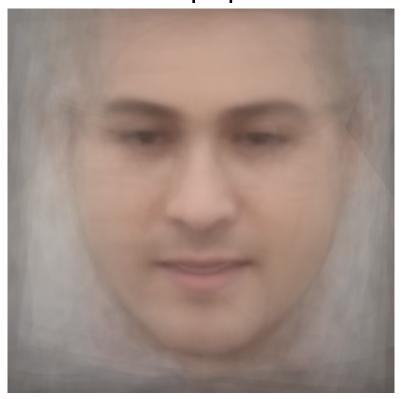
"bulldog owner"



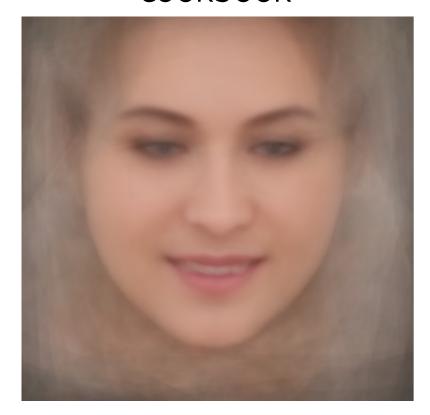
"chihuahua owner"

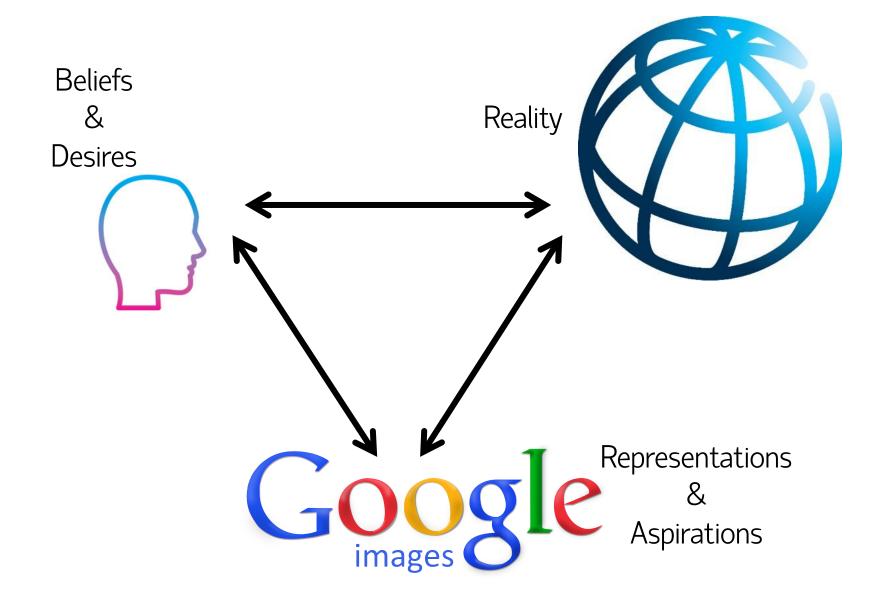


"person reading a newspaper"



"person reading a cookbook"







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The Top Ten Democrats for 2020 | TheHill thehill.com



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2020 presidential election: who's ... vox.com













Summary

People undermine their commitment to egalitarian values by making Bayesian judgments

2. Formalizing "egalitarian values"

3. Google Images as a proxy for the social environment

Closing thoughts

Life is mostly between-subjects.

Make it more within-subjects.

Need for theory on specifying egalitarian principles.

Relatively low-cost tweaks might go a long way towards promoting inclusion.

Thank you



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Jason Mitchell & Jim Sidanius

Research Assistants
Kirsten Morehouse
Juan Lopez Martin



Max Kleiman-Weiner





